

Network-level performance evaluation of a two-relay cooperative random access wireless system

Georgios Papadimitriou, Nikolaos Pappas, Apostolos Traganitis and Vangelis Angelakis

Linköping University Post Print



N.B.: When citing this work, cite the original article.

Original Publication:

Georgios Papadimitriou, Nikolaos Pappas, Apostolos Traganitis and Vangelis Angelakis, Network-level performance evaluation of a two-relay cooperative random access wireless system, 2015, Computer Networks, (88), 187-201.

<http://dx.doi.org/10.1016/j.comnet.2015.06.012>

Copyright: Elsevier

<http://www.elsevier.com/>

Postprint available at: Linköping University Electronic Press

<http://urn.kb.se/resolve?urn=urn:nbn:se:liu:diva-121297>

Network-Level Performance Evaluation of a Two-Relay Cooperative Random Access Wireless System

Georgios Papadimitriou, Nikolaos Pappas, Apostolos Traganitis, Vangelis Angelakis

Abstract

In wireless networks relay nodes can be used to assist the users' transmissions to reach their destination. Work on relay cooperation, from a physical layer perspective, has up to now yielded well-known results. This paper takes a different stance focusing on network-level cooperation. Extending previous results for a single relay, we investigate here the benefits from the deployment of a second one. We assume that the two relays do not generate packets of their own and the system employs random access to the medium; we further consider slotted time and that the users have saturated queues. We obtain analytical expressions for the arrival and service rates of the queues of the two relays and the stability conditions. We investigate a model of the system, in which the users are divided into clusters, each being served by one relay, and show its advantages in terms of aggregate and throughput per user. We quantify the above, analytically for the case of the collision channel and through simulations for the case of Multi-Packet Reception (MPR), and we provide insight on when the deployment of a second relay in the system can yield significant advantages.

I. INTRODUCTION

Cooperative communications have gained significant attention lately. Cooperation can take place in different communication layers, with the bulk of interest focusing on physical layer performance [2], [3]. In that level, cooperation benefits are self-evident, since the explored systems typically belong to a single actor with interest to maximize a specific utility [4]. Promoting cooperation at higher layers, has also drawn significant attention due to the potential benefits from operators and users. Focusing on the purely network layer the benefits of utilizing cooperative techniques have been recently shown to be multi-fold, with respect to system performance in terms of throughput [5]–[10], reliability [11] and delay [8]. In that regard the use of dedicated relays has been introduced in many practical systems, such as wi-fi (known as range extenders) and in LTE.

A. Related Work

The notion of cooperative communications was introduced by information theory with the relay channel. The relay channel is the basic building block for the implementation of cooperative communications, which are widely acknowledged to provide higher communication rates and reliability in a wireless network with time varying channels [3]. It was initially proposed by van der Meulen [12], and its first information-theoretic characterizations were presented in [13].

Recently, the study of the relay channel has gained significant interest in the wireless communications community. In [14] for the classic relay channel a protocol is presented for selection of reception and transmission time slots adaptively and based on the quality of the involved links. Considering full-duplex and half-duplex relaying [15] shows that if the numbers of antennas at source and destination are equal to or larger than the number of antennas at the relay, half-duplex relaying can achieve in some cases higher throughput than ideal full-duplex relaying. With beamforming and taking inter-relay interference [16] proposes two buffer-aided relay selection schemes.

G. Papadimitriou is with Ericsson, Stockholm, Sweden (e-mail: georgios.papadimitriou@ericsson.com). N. Pappas and V. Angelakis are with the Department of Science and Technology, Linköping University, Norrköping SE-60174, Sweden (e-mail: {nikolaos.pappas, vangelis.angelakis}@liu.se). A. Traganitis is with the Computer Science Department, University of Crete, Greece and the Institute of Computer Science, Foundation for Research and Technology - Hellas (FORTH) (e-mail: tragani@ics.forth.gr). This work was presented in part in IEEE ICC 2013 [1].

The research leading to these results has received funding from the People Programme (Marie Curie Actions) of the European Union's Seventh Framework Programme FP7/2007-2013/ under REA grant agreements n° [324515] (MESH-WISE) and n° [612361] (SOrBet).

Interference cancellation is employed in [17] to allow opportunistic relaying selection maximising the average capacity of the network. For a practical system, OFDMA based cellular resource allocation schemes are proposed in [18] for multiple relay stations (RS) with adaptive RS activation.

As mentioned, the majority of the works in this area focus on potential gains by cooperation on the physical layer. Recent works [5] and [6] suggest that similar gains can be achieved by network-layer cooperation. By network-layer cooperation they consider relaying to be taking place at a protocol level avoiding physical layer considerations. Random multiple access schemes in these works use the collision channel model with erasures, where concurrent transmissions will fail [6], [19], [20]. The collision channel however is not the appropriate model for wireless networks.

Random access with Multi-Packet Reception (MPR) capabilities has attracted attention recently [21]–[24]. The seminal paper [21] was the first to examine MPR as an interaction between the physical and medium access control layers for a wireless random access network. In [22], the notion of MPR was introduced and two important theorems for the slotted ALOHA network with MPR are provided. They consider the effect of MPR on stability and delay of slotted Aloha based random-access system and it is shown that the stability region undergoes a phase transition from a concave region to a convex polyhedral region as the MPR capability improves in a two-user system. In [23], the authors specify a general asymmetric MPR model and the medium access control capacity region. In [24], the impact of a relay node to a network with a finite number of users-sources and a destination node is investigated. In this network the relay and the destination nodes have MPR capabilities. Analytical expressions for the characteristics of the relay node queue such as average queue length, stability conditions etc. were obtained. Finally, an overview of MPR-related research work covering the theoretically proved impacts and advantages of using MPR from a channel perspective to network capacity and throughput, the various technologies that enable MPR from transmitter, transceiver, and receiver perspectives and previous work on protocol improvement to better exploit MPR, is provided in [25].

B. Contribution

In this work, we provide a thorough study of the impact of using two relay nodes in a network to assist with relaying packets from a number of users to a destination node. We first investigate the system analytically, assuming the collision channel; then we move to assume that the system is MPR enabled and we conduct a thorough, system-level simulation study. Our common assumptions in both models are that (i) users have saturated queues and random access to the medium with slotted time¹; (ii) the transmission of a packet takes the duration of exactly one time slot; (iii) the two relays are dedicated, i.e. do not have packets of their own, but assist the users by relaying their packets when necessary; (iv) the wireless link between any two nodes of the network is a Rayleigh narrowband flat-fading channel with additive Gaussian noise.

In the first part, we obtain analytical expressions for the arrival and service rates of the queues of the two relays, and for the stability conditions. In doing so we use the stochastic dominance technique [28] because the two queues are coupled (i.e., the service process of each queue depends on the other queue having a packet to send or not). We also look into a topology of the system in which the users are divided into two clusters. In this scenario, we consider that the users of one cluster do not interfere with the users or the relay of the other cluster, still, the relays are interfering with each other. This corresponds to the case of having the users in two distant areas. However, since the location of the users is captured by the link success probability, this scenario can cover any similar case, in which a system practitioner could leverage sophisticated clustering techniques to approach our results, even in an on-line fashion. In general, clustering can deliver results depending on the topology of the users [29]. For both scenarios (with and without clustering) we study the impact of the two relay nodes of the two cases on the aggregate throughput and the throughput per user when the queues of the two relays are stable. We show that the probabilities of the two relays to attempt transmission do not depend on each other when the queues are stable. The insertion of the second relay offers a significant performance gain (higher throughput) when the users are divided into clusters and each cluster is assigned to one relay, though in the general un-clustered scenario the gains are not as significant.

¹Dealing with analytical performance evaluation of random access systems above three users with random arrivals is mathematically intractable. Specifically, assuming the sources saturated, the so-called saturated throughput can be obtained and is an inner bound of the stable throughput [26], [27].

Under the MPR model, the transmission of a node j is successful if the received Signal to Interference plus Noise Ratio (SINR) is above a threshold γ_j . Here, due to queue coupling the stability analysis and the derivation of analytical expressions for the characteristics of the relays' queues such as arrival and service rates, are not tractable. We therefore conduct extensive simulations to provide a comprehensive insight into the performance of the two-relay system. We show that the use of two relays offers significant advantage in terms of aggregate and throughput per user compared to systems with one and no relay, for values of SINR threshold $\gamma > 1$. Under the clustering scenario employed in the first part we study the impact on the aggregate and throughput per user compared to the cases of no relay, one relay and two variations of two relay nodes' operation: a packet received by both relays is either kept by (i) both nodes or (ii) by the one with the smallest queue of the two. Finally, we provide insight for the average queue size and the average delay per packet of the systems presented.

The paper is structured as follows: in Section II we describe the system model. In Section III we derive the analytical expressions for: (A) the arrival and service rate of the relays' queues, (B) the stability conditions of the queues, (C) the stability region and (D) the throughput per user along with the upper and lower bounds. In Section IV we present the numerical and simulation study of the analytically obtained results of Section III, while in section V we conduct a thorough simulation study for the MPR model. We give our conclusions in Section VI.

II. SYSTEM MODEL

A. Network Model

We consider a network with N source users, two relay nodes R_1 and R_2 and a common destination node d , a case for $N = 2$ is depicted in Fig. 1. The sources transmit packets to the destination with the cooperation of the two relays. We assume that the queues of the users are saturated. The users have random access to the medium with no coordination among them. The channel is slotted in time and the transmission of a packet takes the duration of exactly one time slot. We assume fixed packet size, which could be viewed as an average packet size, since taking into account variable packet sizes would severely complicate the analysis. The acknowledgements (ACKs) of successful transmissions are instantaneous and error free. With this set of assumptions, and especially random access of the medium, a host of system parameters that could be available, such as channel state information for the links is not required nor considered in our work.

The relays do not generate packets of their own. If a transmission of a user's packet to the destination fails, the relays store it in their queues and try to forward it to the destination at a subsequent time slot. In case that both relays receive the same packet from a user, they choose randomly and with equal probability which will store it in its queue. The queues at the relays have infinite size.

In this work we consider two cases for the relays and the destination, either that they are equipped with single transceivers thus, a simultaneous transmission attempts by two or more nodes (source-users or relays) result in a collision, or that they are equipped with multiuser detectors, so that they may decode packets successfully from more than one transmitter at a time. The specifics for these are given in the following section.

The notation we consider throughout this paper is the following: The users attempt to transmit with probabilities q_i , where $i = 1, 2, \dots, N$. Each of the relays, having not saturated queues, attempts to transmit with probability q_{R_j} , $j = 1, 2$ if its queue is not empty. Thus probability that a relay will transmit a packet at a time slot t is $q_{R_i} \Pr(Q_{R_i}^t > 0)$, where $i = 1, 2$ and $Q_{R_i}^t$ indicates the size of the queue at time slot t .

B. Physical Layer Model

1) *Collision Channel*: We model the link between two nodes i and j of the network as a Rayleigh narrowband flat-fading channel with additive Gaussian noise. The outage probability of that link with SNR threshold γ_j is known [30] to be $\Pr(SNR_{ij} < \gamma_j) = 1 - \exp(-\gamma_j n_j r_{ij}^\alpha / P_{tx}(i))$ where $P_{tx}(i)$ is the transmission power of node i , r_{ij} is the distance between nodes i and j , α is the path loss exponent and n_j is the power of the additive white Gaussian noise at j . So, by p_{ij} we denote the success probability of a transmission between nodes i and j , which is $p_{ij} = \exp(-\gamma_j n_j r_{ij}^\alpha / P_{tx}(i))$.

The average service rate seen by the relay R_1 is

$$\mu_{R_1} = q_{R_1} p_{R_1 d} [1 - q_{R_2} \Pr(Q_{R_2} > 0)] \prod_{i=1}^N (1 - q_i). \quad (1)$$

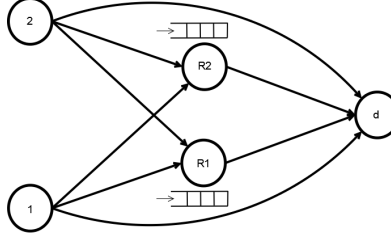


Fig. 1: Two relay nodes with $N = 2$ user nodes.

Because of the collision channel, all the users should remain silent, which is with probability $\prod_{i=1}^N (1 - q_i)$, also the relay R_2 should remain silent, with probability $1 - q_{R_2} \Pr(Q_{R_2} > 0)$. Furthermore, relay R_1 has to be active, with probability q_{R_1} and the transmission to the destination successful with probability $p_{R_1 d}$.

Similarly, the average service rate seen by relay R_2 is

$$\mu_{R_2} = q_{R_2} p_{R_2 d} [1 - q_{R_1} \Pr(Q_{R_1} > 0)] \prod_{i=1}^N (1 - q_i). \quad (2)$$

Since the average service rate of each queue depends on the state of the other, the problem of coupled queues arises. Thus, we will apply the stochastic dominance approach to bypass this difficulty.

2) *MPR*: In the wireless environment, the collision channel is restrictive, since we can not have more than one successful transmissions simultaneously. Thus, we also consider the MPR channel model, which is a generalized form of the packet erasure model [24]. In the MPR case, a node's transmission is successful if the SINR is above a certain threshold. More specifically, if there exists a set of T nodes transmitting in the same time slot and $P_{rx}(i, j)$ is the signal power received from node i at node j (when i transmits), then the SINR(i, j) determined by node j is given by

$$\text{SINR}(i, j) = \frac{P_{rx}(i, j)}{n_j + \sum_{k \in T \setminus \{i\}} P_{rx}(k, j)},$$

where n_j is the receiver noise power at j .

We assume that a packet transmitted by i is successfully received by j if and only if $\text{SINR}(i, j) \geq \gamma_j$, where γ_j is a threshold characteristic of node j . Moreover, the wireless channel is subject to fading. Let $P_{tx}(i)$ be the transmitting power of node i and r_{ij} be the distance between i and j . Then, the power received by j when i transmit is $P_{rx}(i, j) = A(i, j)g(i, j)$, where $A(i, j)$ is a random variable representing channel fading and under Rayleigh fading it is exponentially distributed [30]. The receiver power factor $g(i, j)$ is given by $g(i, j) = P_{tx}(i)r_{ij}^{-\alpha}$, where α is the path loss exponent with typical values between 2 and 4. The average success probability of a packet over link ij when the transmitting nodes are in T is given by [30]

$$P_{i/T}^j = \exp\left(-\frac{\gamma_j \eta_j}{v(i, j)g(i, j)}\right) \prod_{k \in T \setminus \{i, j\}} \left(1 + \gamma_j \frac{v(k, j)g(k, j)}{v(i, j)g(i, j)}\right)^{-1},$$

where $v(i, j)$ is the parameter of the Rayleigh random variable for fading.

Remark 1. In this work, the MPR case is considered only with simulations since the analytical expressions even for the case of one relay are rather complicated [24]. Additionally, with small values of the SINR threshold γ is more likely to have more successful simultaneous transmissions comparing to larger γ . More specifically, if $\gamma < 1$ it is possible for two or more users to transmit successfully at the same time, comparing to $\gamma > 1$ which that probability is almost zero in the considered system setup.

C. Queue Stability

We adopt the definition of queue stability used in [31].

Definition 1. Denote by Q_i^t the length of queue i at the beginning of timeslot t . The queue is said to be stable if

$$\lim_{t \rightarrow \infty} \Pr[Q_i^t < x] = F(x) \text{ and } \lim_{x \rightarrow \infty} F(x) = 1.$$

If $\lim_{x \rightarrow \infty} \lim_{t \rightarrow \infty} \inf \Pr[Q_i^t < x] = 1$, the queue is substable. If a queue is stable, then it is also substable. If a queue is not substable, then we say it is unstable.

Loynes' theorem [32] states that if the arrival and service processes of a queue are strictly jointly stationary and the average arrival rate is less than the average service rate, then the queue is stable.

III. ANALYSIS

In this section we will present the analysis for the collision channel model. We obtain analytical equation for the arrival and the service rate of the two relays and also the stability region of the system. Additionally, we obtain the throughput per user as well as the aggregate throughput of the system.

In order to proceed further we need to calculate the average arrival rates at the queues of the relays.

There is an arrival at the queue of relay R_1 if both relays are silent, only one user transmits, and its transmission is successfully received by R_1 but not by the destination. When both relays receive the packet then the first will store it in its queue with probability $\frac{1}{2}$ otherwise the second relay will store it.

The probability that both relays are silent depends on the state of the queues at the relays. Both relays are silent when their queues are empty, which happens with probability $\Pr(Q_{R_1} = 0, Q_{R_2} = 0)$, when the i relay has a non-empty queue but the queue at the $j \neq i$ relay is empty then the probability that both relays are silent is $(1 - q_{R_i})\Pr(Q_{R_i} > 0, Q_{R_j} = 0)$. The probability that both relays are silent when their queues are not empty is $(1 - q_{R_1})(1 - q_{R_2})\Pr(Q_{R_1} > 0, Q_{R_2} > 0)$. The average arrival rate at the first relay, λ_{R_1} , is

$$\begin{aligned} \lambda_{R_1} = & [\Pr(Q_{R_1} = 0, Q_{R_2} = 0) + (1 - q_{R_1})\Pr(Q_{R_1} > 0, Q_{R_2} = 0) + (1 - q_{R_2})\Pr(Q_{R_1} = 0, Q_{R_2} > 0) + \\ & + (1 - q_{R_1})(1 - q_{R_2})\Pr(Q_{R_1} > 0, Q_{R_2} > 0)] \sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \left[(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2} \right] \prod_{j=1, j \neq i}^N (1 - q_j), \end{aligned} \quad (3)$$

which after simple manipulation becomes

$$\begin{aligned} \lambda_{R_1} = & [1 - q_{R_2}\Pr(Q_{R_2} > 0) - q_{R_1}\Pr(Q_{R_1} > 0) - q_{R_1}q_{R_2}\Pr(Q_{R_1} > 0, Q_{R_2} > 0)] \times \\ & \times \sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \left[(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2} \right] \prod_{j=1, j \neq i}^N (1 - q_j). \end{aligned} \quad (4)$$

Symmetrically, we have that the arrival rate at the second relay, λ_{R_2} , is

$$\begin{aligned} \lambda_{R_2} = & [1 - q_{R_1}\Pr(Q_{R_1} > 0) - q_{R_2}\Pr(Q_{R_2} > 0) - q_{R_1}q_{R_2}\Pr(Q_{R_1} > 0, Q_{R_2} > 0)] \times \\ & \times \sum_{i=1}^N q_i p_{iR_2} (1 - p_{id}) \left[(1 - p_{iR_1}) + \frac{1}{2} p_{iR_1} \right] \prod_{j=1, j \neq i}^N (1 - q_j). \end{aligned} \quad (5)$$

With the previous expressions for λ_{R_1} and λ_{R_2} we cannot proceed further, since each rate depends on the joint probability density function of the queues. This is a well known non-tractable problem, and in order to bypass this difficulty we will deploy the stochastic dominance technique [28] in order to decouple the queues. The stochastic dominance technique was initially developed to overcome the intractability arising in the analysis of the inseparable multidimensional Markov chain for finite-user buffered slotted ALOHA².

A. Computation of Arrival and Service Rate

The stochastic dominance approach implies the construction of two hypothetical dominant systems. In the first system, say \mathcal{S}_1 , the relay R_1 reverts to the transmission of "dummy packets" with the same probability, when its queue is empty. All the other characteristics and assumptions of the original system remain exactly the same. Similarly, in the second system \mathcal{S}_2 the relay R_2 reverts to the transmission of "dummy packets" with the same probability, when its queue is empty.

²The stochastic dominance technique was introduced in [28] however, a brief introduction can be found in [33].

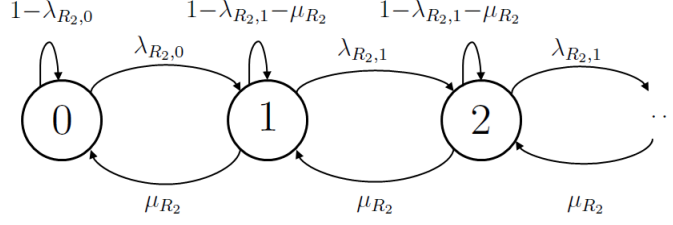


Fig. 2: The Discrete Time Markov Chain model of the queue at the relay R_2 for the first dominant system \mathcal{S}_1 .

1) Dominant system \mathcal{S}_1 – Relay R_1 transmits “dummy packets”: In the first dominant system, the relay R_1 transmits “dummy packets” when its queue is empty, thus $\Pr(Q_{R_1} > 0) = 1$. The average arrival rates λ_{R_1} and λ_{R_2} are

$$\lambda_{R_1} = (1 - q_{R_1}) [1 - q_{R_2} \Pr(Q_{R_2} > 0)] \sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \left[(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2} \right] \prod_{j=1, j \neq i}^N (1 - q_j) \quad (6)$$

$$\lambda_{R_2} = (1 - q_{R_1}) [1 - q_{R_2} \Pr(Q_{R_2} > 0)] \sum_{i=1}^N q_i p_{iR_2} (1 - p_{id}) \left[(1 - p_{iR_1}) + \frac{1}{2} p_{iR_1} \right] \prod_{j=1, j \neq i}^N (1 - q_j). \quad (7)$$

The service rate of the relay R_2 in the system \mathcal{S}_1 is given by

$$\mu_{R_2} = q_{R_2} p_{R_2d} (1 - q_{R_1}) \prod_{i=1}^N (1 - q_i), \quad (8)$$

and μ_{R_1} is given by (1). The probability that the queue at the R_2 is not empty is $\Pr(Q_{R_2} > 0) = \frac{\lambda_{R_2}}{\mu_{R_2}}$ which can be obtained from Little’s law. However, since the average arrival rate for the second relay, λ_{R_2} , depends on the $\Pr(Q_{R_2} > 0)$ we cannot directly apply the previous expression. Furthermore, λ_{R_1} and the service rate μ_{R_1} depend on the state of the queue of the second relay. Thus, we follow the procedure described in [19]. We model the queue at the R_2 as a Discrete Time Markov Chain (DTMC) with infinite states in order to describe the queue evolution. The DTMC is depicted in Fig. 2. The arrival rate of relay R_2 depends on whether its queue is empty or not. If the queue is empty the arrival rate is denoted by $\lambda_{R_2,0}$ and by $\lambda_{R_2,1}$ if it is not. Thus, the average arrival rate λ_{R_2} can be expressed also as

$$\lambda_{R_2} = \Pr(Q_{R_2} = 0) \lambda_{R_2,0} + \Pr(Q_{R_2} > 0) \lambda_{R_2,1}. \quad (9)$$

If the queue at the relay R_2 is empty then, we can easily show that the probability of arrival $\lambda_{R_2,0}$ is

$$\lambda_{R_2,0} = (1 - q_{R_1}) \sum_{i=1}^N q_i p_{iR_2} (1 - p_{id}) \left[(1 - p_{iR_1}) + \frac{1}{2} p_{iR_1} \right] \prod_{j=1, j \neq i}^N (1 - q_j). \quad (10)$$

If the queue is not empty then the arrival rate is

$$\lambda_{R_2,1} = (1 - q_{R_2}) \lambda_{R_2,0}. \quad (11)$$

By following the same methodology as in [19] and applying the method of balance equations, we can compute the stationary distribution of the states i . The stationary distribution of the Markov Chain exists if and only if $\lambda_{R_2,1} < \mu_{R_2}$. Thus, the probability that the queue at the R_2 is empty is given by

$$\Pr(Q_{R_2} = 0) = \frac{\mu_{R_2} - \lambda_{R_2,1}}{\mu_{R_2} - \lambda_{R_2,1} + \lambda_{R_2,0}}. \quad (12)$$

From (10), (11), (12) and (9) we obtain

$$\lambda_{R_2} = \frac{\mu_{R_2} \lambda_{R_2,0}}{\mu_{R_2} - \lambda_{R_2,1} + \lambda_{R_2,0}}. \quad (13)$$

Combining (9), (10), (11) and (13) we obtain the expression of the arrival rate λ_{R_2} , shown in (14), from which we see that λ_{R_2} does not depend on q_{R_2} , the probability of transmission of R_2 .

$$\lambda_{R_2} = \frac{p_{R_2d} \prod_{i=1}^N (1 - q_i) [\sum_{i=1}^N q_i p_{iR_2} (1 - p_{id}) (1 - q_{R_1}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_1}) + \frac{1}{2} p_{iR_1}]]}{p_{R_2d} \prod_{i=1}^N (1 - q_i) + \sum_{i=1}^N q_i p_{iR_2} (1 - p_{id}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_1}) + \frac{1}{2} p_{iR_1}]}. \quad (14)$$

2) *Dominant system S_2 – Relay R_2 transmits “dummy packets”*: By following exactly the same procedure as in system S_1 , we obtain the expressions for μ_{R_1} , λ_{R_1} , μ_{R_2} and λ_{R_2} .

B. Necessary and Sufficient Stability Conditions

The stability region of the system is defined as the set of arrival rate vectors $(\lambda_{R_1}, \lambda_{R_2})$ for which the queues in the system are stable. In order to derive the stability region we need to characterize the average arrival rates λ_{R_1} and λ_{R_2} as well as the average service rates μ_{R_1} and μ_{R_2} . A tool to obtain stability condition for a queue is the Loyne’s criterion [32], which states that if the arrival rate is less than the service rate then the queue is stable. The average service rates are given by (1) and (2) thus the service rate of each queue depends on the state of the other, thus we cannot apply the Loyne’s criterion directly. We will apply the stochastic dominance technique, which was presented in the previous subsection for decoupling the queues and to obtain necessary and sufficient conditions for the stability. Recall that there are two dominant systems S_1 and S_2 . In S_i where in the relay R_i transmits dummy packets when its queue is empty and all the other assumptions remain unaltered. Note that the expressions for the average arrival and service rates change from one dominant system to another since they depend on the probability that a queue is empty.

In the first dominant system S_1 , we have that the queues are stable if $\lambda_{R_1} < \mu_{R_1}$ and $\lambda_{R_2} < \mu_{R_2}$. The expression for the service rate μ_{R_2} is given by (8) and the service rate μ_{R_1} by (1). Thus, using Little’s law we obtain that

$$\Pr(Q_{R_2} > 0) = \frac{\lambda_{R_2}}{q_{R_2} p_{R_2d} (1 - q_{R_1}) \prod_{i=1}^N (1 - q_i)}. \quad (15)$$

After replacing (15) into (1) we obtain that

$$\mu_{R_1} = q_{R_1} p_{R_1d} \left(1 - q_{R_2} \frac{\lambda_{R_2}}{q_{R_2} p_{R_2d} (1 - q_{R_1}) \prod_{i=1}^N (1 - q_i)} \right) \prod_{i=1}^N (1 - q_i). \quad (16)$$

Now we can apply Loyne’s criterion for both queues and obtain the region \mathcal{R}_1 from the first dominant system which is given by

$$\mathcal{R}_1 = \left\{ (\lambda_{R_1}, \lambda_{R_2}) : \lambda_{R_1} < q_{R_1} p_{R_1d} \left(1 - q_{R_2} \frac{\lambda_{R_2}}{q_{R_2} p_{R_2d} (1 - q_{R_1}) \prod_{i=1}^N (1 - q_i)} \right) \prod_{i=1}^N (1 - q_i), \right. \\ \left. \lambda_{R_2} < q_{R_2} p_{R_2d} (1 - q_{R_1}) \prod_{i=1}^N (1 - q_i) \right\}. \quad (17)$$

From the above condition and after using (6), (7) and (14) we can further obtain the expression for the transmission probability, q_{R_1} where

$$q_{R_1} > q_{R_1, \min} \Leftrightarrow q_{R_1} > \frac{\sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2}]}{\sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2}] + p_{R_1d} \prod_{i=1}^N (1 - q_i)}. \quad (18)$$

So, the $q_{R_1, \min}$ for which the queue is stable is given by

$$q_{R_1, \min} = \frac{\sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2}]}{\sum_{i=1}^N q_i p_{iR_1} (1 - p_{id}) \prod_{j=1, j \neq i}^N (1 - q_j) [(1 - p_{iR_2}) + \frac{1}{2} p_{iR_2}] + p_{R_1d} \prod_{i=1}^N (1 - q_i)}. \quad (19)$$

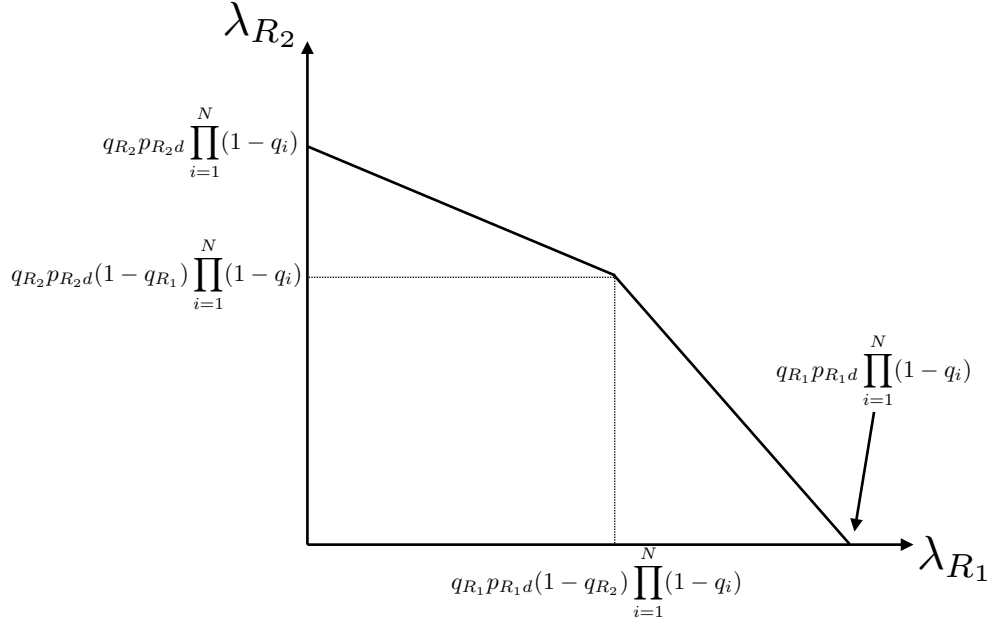


Fig. 3: The stability region, \mathcal{R} , of the system. The boundaries of the region are given by (17) and (20).

From the second dominant system, \mathcal{S}_2 , symmetrically we obtain the stability region \mathcal{R}_2 .

$$\mathcal{R}_2 = \left\{ (\lambda_{R_1}, \lambda_{R_2}) : \lambda_{R_2} < q_{R_2} p_{R_2} d \left(1 - q_{R_1} \frac{\lambda_{R_1}}{q_{R_1} p_{R_1} d (1 - q_{R_2}) \prod_{i=1}^N (1 - q_i)} \right) \prod_{i=1}^N (1 - q_i), \right. \\ \left. \lambda_{R_1} < q_{R_1} p_{R_1} d (1 - q_{R_2}) \prod_{i=1}^N (1 - q_i) \right\}. \quad (20)$$

Following exactly the same procedure as in \mathcal{S}_1 we obtain expressions and bounds for q_{R_2} , and $q_{R_2, \min}$ similar to (18) and (19) respectively with R_1 and R_2 interchanged. Similarly to system \mathcal{S}_1 , we observe that q_{R_2} does not depend on q_{R_1} . The queue of the relay R_2 is stable if q_{R_2} satisfies the inequality

$$q_{R_2, \min} < q_{R_2} < 1. \quad (21)$$

Finally the stability region of the system, \mathcal{R} , is $\mathcal{R} = \mathcal{R}_1 \cup \mathcal{R}_2$ and is shown in Fig. 3.

It is interesting to note that in [28], the stability conditions obtained by the dominant systems are not merely sufficient, but sufficient and necessary for the stability of the original system. The proof relies on the *indistinguishability* argument which also applies in our case. By considering the properties of the dominant system \mathcal{S}_1 , we can see that the queue sizes of the two relays cannot be smaller than those in the original system, provided the queues start with identical initial conditions in both systems. By Loynes' Theorem, the stability condition of a queue is given by $\lambda < \mu$. Therefore, given that $\lambda_{R_2} < \mu_{R_2}$, if for some λ_{R_1} the queue R_1 in the dominant system \mathcal{S}_1 is stable, then the queue is also stable in the original system. Conversely, if for some λ_{R_1} in the dominant system \mathcal{S}_1 the queue R_1 is unstable, then it will not transmit any “dummy packets” and as long as the queue does not empty, the dominant and the original systems behave identically and as a consequence, the queue is unstable in the original system as well.

C. Throughput Per User

In this part, we will give the expression for the average user throughput, which is the average rate of packets departing from each user. There is a departure of a packet from a node if it transmits whereas the two relays and all the other users are silent, and its transmission is either successfully received by the destination or if unsuccessful,

it is successfully received by R_1 or R_2 . Thus, the throughput rate μ_i seen by the user i is

$$\begin{aligned} \mu_i = q_i [p_{id} + (1 - p_{id})(p_{iR_1} + p_{iR_2} - p_{iR_1}p_{iR_2})] [\Pr(Q_{R_1} = 0, Q_{R_2} = 0) + (1 - q_{R_1})\Pr(Q_{R_1} > 0, Q_{R_2} = 0) + \\ + (1 - q_{R_2})\Pr(Q_{R_1} = 0, Q_{R_2} > 0) + (1 - q_{R_1})(1 - q_{R_2})\Pr(Q_{R_1} > 0, Q_{R_2} > 0)] \prod_{j=1, j \neq i}^N (1 - q_j), \end{aligned} \quad (22)$$

which, after some simplifications is given by

$$\begin{aligned} \mu_i = q_i [p_{id} + (1 - p_{id})(p_{iR_1} + p_{iR_2} - p_{iR_1}p_{iR_2})] \times \\ \times [1 - q_{R_2}\Pr(Q_{R_2} > 0) - q_{R_1}\Pr(Q_{R_1} > 0) - q_{R_1}q_{R_2}\Pr(Q_{R_1} > 0, Q_{R_2} > 0)] \prod_{j=1, j \neq i}^N (1 - q_j). \end{aligned} \quad (23)$$

We observe that the throughput per user depends on whether both queues are empty or not. So, it is not tractable to find an explicit expression of the throughput per user in closed form. Instead, we will find an upper and a lower bound and by simulation we will study the tightness of these bounds.

In order to find an upper bound, we will consider the case when the two relays do not interfere with the users. This provides an upper bound because if the relays do not interfere with the users, the interference in the system is less and thus we get higher throughput per user. This is the case when we assume that the relays operate in a different channel than the users. This upper bound is given by

$$\mu_{i,upper} = q_i [p_{id} + (1 - p_{id})(p_{iR_1} + p_{iR_2} - p_{iR_1}p_{iR_2})] \prod_{j=1, j \neq i}^N (1 - q_j). \quad (24)$$

In order to find a lower bound, we will assume that the two relays have always packets in their queues, their queues never empty. This can be the case when the relays are highly utilized. The lower bound is given by

$$\mu_{i,lower} = \mu_{i,upper}(1 - q_{R_1})(1 - q_{R_2}). \quad (25)$$

However, the way we treated the relays so far, that can be reached from any user, can be sub-optimal thus, in the following subsection we consider the case of using one relay per cluster of users.

D. Improving the Throughput Per User by Clustering Users

In order to improve the throughput per user of the system, we consider the case that we divide the users into two clusters served by relays R_1 and R_2 . We assume that due to the distance between clusters the users of the first cluster do not interfere with the users of the second cluster at their relay. If two users transmit simultaneously we will have a collision at the destination. We also assume that when a relay transmits simultaneously with the users, the users' transmissions do not affect the relay's transmission to the destination node whereas their transmissions to the destination fail. That is because of the shorter distance between the relay and the destination and also the higher transmit power of the relay compared to that of the users'. Furthermore, when both relays transmit simultaneously we have a collision at the destination. We divide the users equally to both clusters and we assume that each cluster has N_k users with $k = 1, 2$ where $N_1 = N_2 = \frac{N}{2}$.

The throughput per user of the system described depends again on whether both queues are empty or not. Thus, we find an upper and a lower bound and we will show that the results of the simulation of that system lie between those two bounds. The upper bound of the throughput per user i of cluster k is given by:

$$\mu_{i,k,upper} = q_i p_{id} \prod_{j=1, j \neq i}^N (1 - q_j) + q_i (1 - p_{id}) p_{iR_k} \prod_{j=1}^{N_k} (1 - q_j). \quad (26)$$

The lower bound for the throughput is given by

$$\mu_{i,k,lower} = \mu_{i,k,upper}(1 - q_{R_1})(1 - q_{R_2}). \quad (27)$$

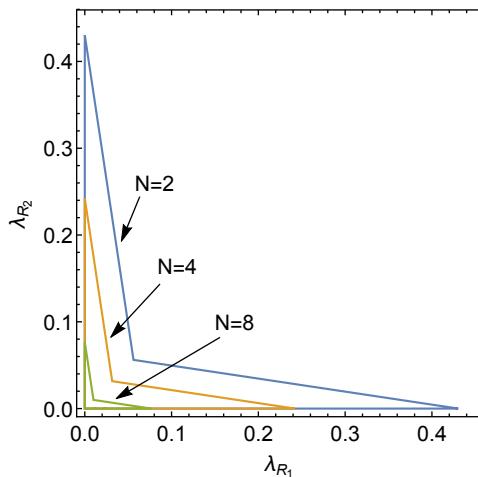


Fig. 4: The stability region of the system described in Table I for $N = 2, 4, 8$ users.

Remark 2. As presented earlier, the throughput per user is given by (23). In order to obtain the inner bounds given by (25) and (27) we did the assumption that the relays have saturated queues. These bounds become tight when the relays' queues approach saturation. The outer bounds for the throughput can be obtained by assuming that the relays' queues are always empty thus, the relays do not cause interference to the users' transmissions. Apparently, the obtained outer bounds are tight when the queues at the relays are underutilized.

IV. NUMERICAL AND SIMULATION RESULTS FOR THE COLLISION CHANNEL MODEL

In this section, we present the numerical results for the per user and aggregate throughput of the system with two stable relays for the collision channel model. We directly verify (in Fig. 5) that the throughput per user for the cases of two relays lies between the upper and lower bounds given in (22)-(25). Then, we compare these two cases with the system without relay and the system with one relay. The results presented below are averages of at least 10,000 runs on each scenario verifying the accuracy of the analysis in the previous sections. We consider that all N users and both the relays have the same link characteristics and transmission probabilities for both the simple and the scenario with user clustering. All parameters in our testing are given in Table I.

The stability region for the considered scenario for $N = 2, 4, 8$ users is depicted in Fig. 4. As the number of users increases we see that the boundary of the region shrinks, which is expected since the number of collisions increases in the network.

A. Throughput Per User

The plots of Fig. 5 present the throughput per user versus the number of users of the “simple” scenario described in Section III-C and the “clustering” scenario of Section III-D. As expected the simulations lie between the lower and the upper bounds defined in previous sections. In Fig. 5a, when the number of the users in the system increases, we see that the throughput per user tends to the lower bound. This is because the relays' queues are approaching saturation as the number of users increases. In this case the lower bound becomes tight.

In Fig. 5b, the throughput per user tends to the upper bound, because the relays' queues tend to be empty most of the time. Thus, we have a better utilization of the system with clustering due to the reduction of concurrent transmissions per relay resulting in less collisions. Furthermore, one can observe in the simulation curves, the result of orthogonalizing user transmissions to the relays via clustering as an effective doubling of the throughput for more than 4 users.

B. The Benefit of Using a Second Relay

The plots of Fig. 6 present the per user and aggregate throughput versus the number of users for the cases of no relay, one relay and two relays (with and without clustering), obtained by simulation. We observe that the simple system with two relays does not offer any advantage over the system with one relay. This is expected because the

TABLE I: Parameters for the collision channel model results.

Notation	Explanation	Value in “Simple” Scenario	Value in “Clustering” Scenario
$p_{iR_j}, i = 1, \dots, N, j = 1, 2$	Success probability of transmission from user i to relay j	$p_{iR_1} = p_{iR_2} = 0.9, i = 1 \dots N$	$p_{iR_1} = p_{jR_2} = 0.9, i = 1 \dots N_1, j = 1 \dots N_2$
$p_{R_jd}, j = 1, 2$	Success probability of transmission from relay j to the destination	$p_{R_jd} = 0.9, j = 1, 2$	
$p_{id}, i = 1, \dots, N$	Success probability of transmission from user i to the destination	$p_{id} = 0.25$	
$q_{R_j}, j = 1, 2$	Probability that relay attempts to transmit in a timeslot, (if its queue is not empty)	$q_{R_1} = q_{R_2} = 0.85$	
$q_i, i = 1, \dots, N$	Probability that user i attempts to transmit in a timeslot	$q_i = 0.25, i = 1, \dots, N$	

insertion of a second relay with high probability to attempt transmission, when its queue is not empty, generates more interference in the system. However, this interference is alleviated in the clustering scenario which thus offers significant advantage over the system with one relay (more than 300% higher aggregate throughput in our specific setup).

C. Average Per Packet Delay

Another important parameter in cooperative systems is the average delay per packet. By delay we refer to the time it takes from the moment a packet has been transmitted until it is delivered to the destination. This parameter is important especially in delay-sensitive networks for real-time services. Thus, here we investigate the average delay per packet of systems with two relays and compare it with the systems with one and no relay.

Fig. 7 presents the average delay per packet (counted in timeslots) versus the number of users for the cases of no relay, one relay and two relays (with and without clustering), obtained by simulation.

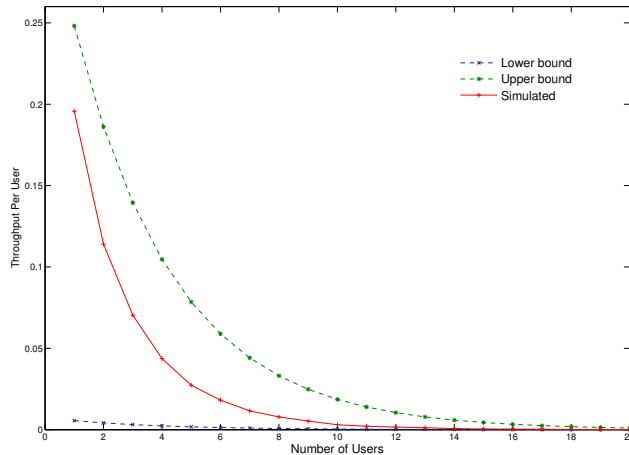
The clustered system with two relays provides the lowest average delay compared to the other systems. Furthermore, the clustered systems appears to be more prone to the increase of the number of the users. Above eight users, the no relay system faces lower average delay than the one and the simple two-relay systems. The reason is that the system without relay does not suffer from additional delays introduced by packets queueing at the relay; this queueing delay increases with the number of users affecting the average per packet delay.

V. SIMULATION RESULTS FOR THE MPR MODEL

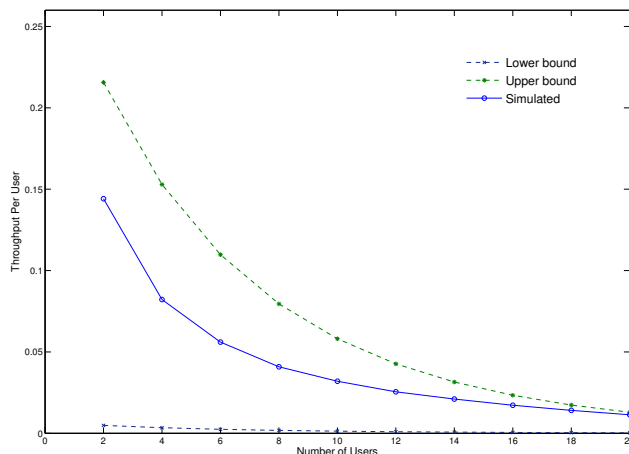
A. The Performance Benefits of Using a Second Relay

Here we present the aggregate and throughput per user for the cases with no relay, one relay, and two relays in the system for the system with MPR, under different values of an assumed SINR threshold γ . We examine two strategies to handle a user’s packet successfully received at both relays: either that **(a)** both relays will store and forward it to the destination (*Simple*) or that **(b)** the packet is stored by the relay which has the smaller queue size (*Smaller Queue Stores Packet*). If the queue size of the two relays is equal, then the two relays choose randomly and with equal probability which one will store the packet in its queue. Furthermore, as we previously did for the collision channel model we also study the potential impact of dividing the users into two clusters served by relays R_1 and R_2 .

An example topology of a two-relay test network with N collocated users is depicted in Fig. 8. The parameters used in the simulations for each of the three cases are shown in Table II. To simplify the presentation, we consider that all users have the same transmission probabilities and all links to have the same SINR threshold γ . Note that,



(a) “Simple” Scenario



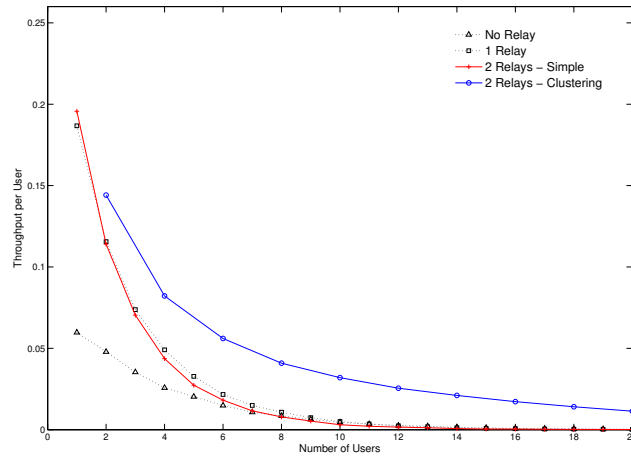
(b) “Clustering” Scenario

Fig. 5: Throughput per user vs. the number of users.

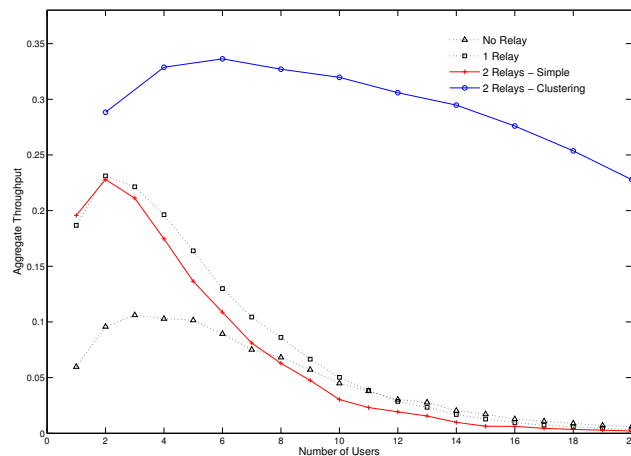
with small values of γ it is more likely to have more successful simultaneous transmissions comparing to larger γ . For $\gamma < 1$ the probability for two or more nodes to transmit successfully at the same time is higher than the same probability when $\gamma > 1$, which tends to zero [24].

We note the assumptions made in our simulations. First, that the path loss exponent between users-destination as well as between the two relays is 4 while between users-relays and relays-destination is taken to be 2. This so that the relay nodes are more accessible for the users than the destination node. Thus we consider user-relay and user-destination channels that are more reliable than the user-destination one. Otherwise, the presence of the relays would degrade the performance of the network [24]. We also assume that the transmit power of the relays is five times higher than that of the users. For the “Smaller Queue Stores Packet” strategy, we assume that the relays communicate in a separate channel and thus these transmissions do not interfere with those of the system we study. For the clustering scenario, we divide the users equally to both clusters and assume that relay R_1 cannot receive packets from users of cluster 2 and relay R_2 cannot receive packets from users of cluster 1 respectively, this is achieved by first taking the respective path loss exponents to be equal to 4 and the distance between cluster 1 and relay R_2 to be 1.5 times the distance between cluster 1 and relay R_1 , and vice-versa.

For a low SINR threshold value ($\gamma = 0.2$), the aggregate throughput (Fig. 9a) and the throughput per user (Fig. 10a) obtained from the system with two relays are consistently, albeit slightly, higher compared to that of one relay.



(a) Throughput per user



(b) Aggregate throughput

Fig. 6: Comparisons of throughput vs. number of users, with the Simple and Clustering Scenarios, against one relay and no relay.

For the aggregate throughput, this gain increases as more users are inserted in the system. However, it is noteworthy that without relays, the system outperforms those with relay(s) regardless of clustering or forwarding strategy, for 8 users and up to a little over 45 users. For more than that, the performance (always in terms of aggregate and throughput per user) by the system with two relays is higher compared to the system with no relay and increases as more users are inserted in the system. Enabling clustering of users in the two relays starts providing clear benefits over 30 users, by an approximate 15%.

Unlike the limited performance gains observed under $\gamma = 0.2$ with the higher SINR thresholds (Figs. 9b and 10b for $\gamma = 1.2$, and 9c and 10c for $\gamma = 2.5$) we observe that the system with two relays offers significant advantage compared to the networks without or with one relay. This is expected since for higher values of γ the relays, having better channel conditions than the destination, receive a larger percentage of the transmitted packets in their queues to forward to the destination. Regarding the forwarding strategy (be it “Simple” or the “Smaller Queue Stores Packet”), across the threshold value there is a common trend that for a few users (less than 10 in low γ , while less than almost 20 in higher γ values) the latter strategy outperforms the simple one. Furthermore, with two relays and clustering, in higher SINR thresholds significant advantages are observed, for over about 10 users. This is again expected because in each cluster the users interfere with only half the users of the system in to successfully reach

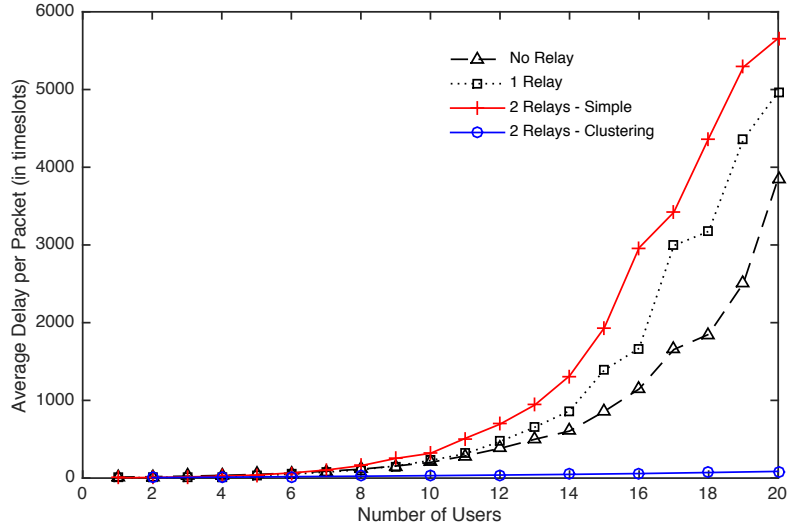


Fig. 7: Comparison of average per packet delay (in timeslots) vs. number of users, with Simple and Clustering scenarios, against one relay and no relay.

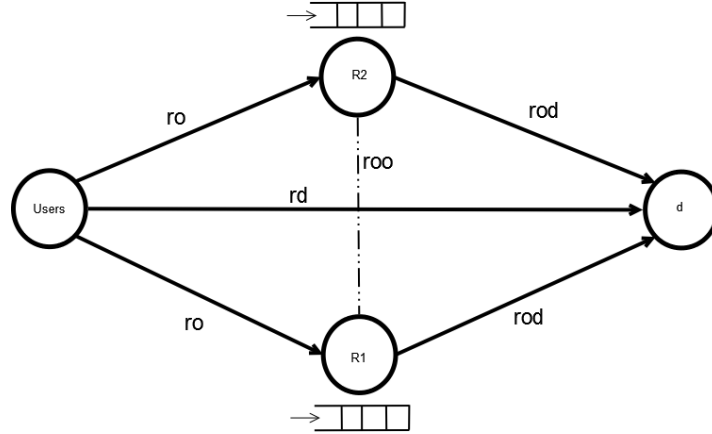


Fig. 8: Two relay nodes with N users with same link characteristics and transmission probabilities.

the corresponding relay (the interference caused in each cluster's relay, by the users of the other cluster is almost negligible due to the distance and channel properties).

Note that, the behavior trends across the four relaying schemes remains stable above $\gamma = 1.2$, in both aggregate throughput and throughput per user. With this in mind, taking a system design perspective, one can finally point out that given the link characteristics and the transmission probabilities, all relaying schemes reach a maximum aggregate throughput, thus depending on the number a system is expected to serve, the network designer can deploy the most appropriate relaying scheme.

B. Average Queue Size

In cooperative systems with relays, a key parameter to be taken into account is the queue size of the relays. It is important not only to keep the queues of the relays stable but also to keep their sizes as low as possible to limit delays.

The plots of Fig. 11 present the average queue size (in packets) versus the number of users for the systems with one and two relays studied in previous sections for $\gamma = 0.2$ up to $\gamma = 2.5$. For the systems with two relays only the average queue size of the one relay is presented (the average queue size of the second is almost equal because we assume that we have symmetric users in the systems).

The plots in the figure show that the average queue size of the clustered system is higher compared to the other systems for a number of users that reduces with the increase of the threshold γ . This is expected because as each

TABLE II: Simulation parameters for the MPR model results.

<i>Notation</i>	<i>Explanation</i>	<i>Value</i>
r_d	users-destination distance	100m
r_R	users-relays distance	59m
$r_{R'}$	clustered user-non-serving relay distance	88m
r_{0d}	relays-destination distance	59m
r_{00}	inter-relay distance	60m
α_{id}	users-destination path loss exponent	4
α_{i0}	users-relays path loss exponent	2
α_{0d}	relays-destination path loss exponent	2
$P_{tx}(i), i = 1 \dots N$	Transmit power of user i	1mW
$P_{tx}(R_j), j = 1, 2$	Transmit power of each relay	5mW
$q_i, i = 1 \dots N$	Probability that user i attempts to transmit in a timeslot	$q_i = 0.25, i = 1 \dots N$
$q_{R_j}, j = 1, 2$	Probability that relay j attempts to transmit in each timeslot (if its queue is not empty)	$q_{R_1} = q_{R_2} = 0.85$

relay serves half the users of the system, the interference between them in the corresponding relay is lower and more simultaneous transmissions to a relay may be successful in a time slot. In that way, the two relays receive more packets resulting in higher queue sizes. It is interesting though to note that the maximum average queue size of the system is below one packet, for the two higher threshold values (about 0.65 packets for $\gamma = 1.2$ and 0.6 for $\gamma = 2.5$). Moreover, in these cases the average queue sizes of the other three systems tend to become equal with over 25 users.

C. Average per Packet Delay

Fig. 12 presents the average delay per packet (counted in timeslots) versus the number of users, for $\gamma = 0.2$ up to $\gamma = 2.5$ for the five relaying cases presented in the previous sections. As expected, with more users inserting packets into the system, the average delay per packet increases due to the increased interference. Figs. 12b and 12c show that the systems with two relays provide less average delay, compared to the systems with one and no relay, when the number of users is larger than 10. Specifically, for 30 users and $\gamma = 1.2$ in Fig. 12b, the clustered system offers the lowest average delay per packet and it is interesting to note that whereas its value increases as the number of users also increases, it does not exceed 50 timeslots, while for the two other cases with two relays its value is about 150 timeslots and for the one relay 240 timeslots and for no relay 900 timeslots. We can make similar observations from Fig. 12c.

Furthermore, the average delay per packet for all the cases except the clustered one increases excessively, for more than 30 users when $\gamma = 1.2$ and 25 users when $\gamma = 2.5$ respectively. Also, due to the fact that the aggregate throughput is fairly low and tends to zero as the number of users tend to 50 (see Figs. 9b and 9c), there are not enough samples in order to make an accurate calculation of the average delay per packet. However, the simulation showed that the average delay per packet obtained from the clustered system for 50 users and $\gamma = 1.2$ is no more than 160 timeslots and for 50 users and $\gamma = 2.5$ it is no more than 460 timeslots.

VI. CONCLUSIONS

In this paper, we examined the potential gains of utilizing two relay nodes to aid the communication of a number of users to a common destination by re-transmitting (when necessary) their packets. Under the classic collision channel model we obtained analytical expressions for the arrival and service rates of the queues of the two relays and

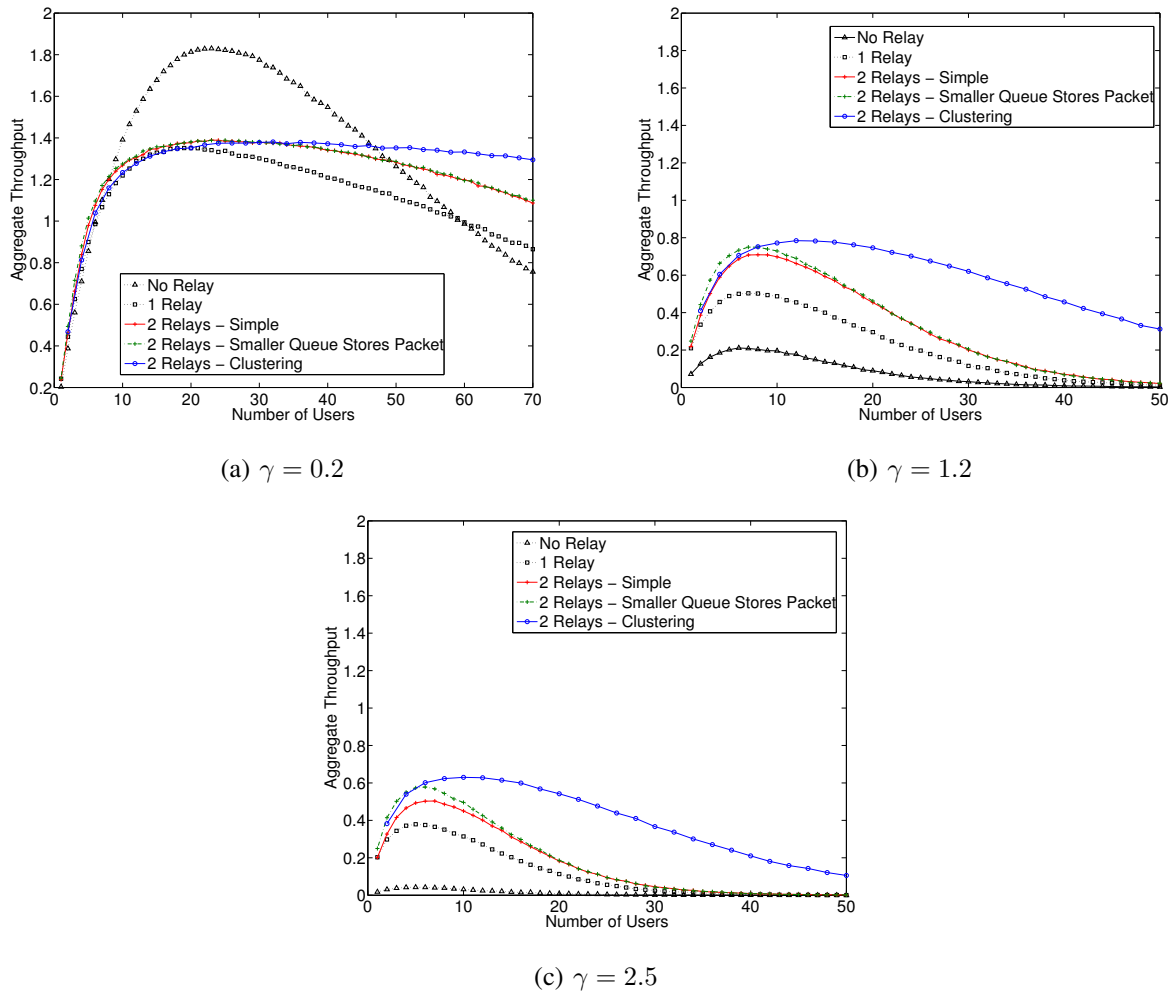


Fig. 9: Aggregate throughput (in packets per slot) vs. the number of users, for different SINR threshold γ values.

also the stability conditions. We further showed that the two relays are free to choose their transmission probabilities independently from each other, provided that these are greater from some minimum values which guarantee the stability of their queues. Employing multi-packet reception made the system intractable, so we conducted a thorough simulation study.

Under both models, we presented a user clustering scenario where the users are divided into two groups, each served by one relay and studied the impact of clustering on the per user and aggregate throughput. Although the insertion of a second relay in a system generally does not offer significantly higher throughput per user in comparison to a system with one relay, the clustered system offers impressive performance gains, in terms of throughput, for large numbers of served users.

Furthermore under the MPR model, we presented two relaying strategies: a simple one, where if both relays receive the same packet they both store it and forward it to the destination, and the Smaller Queue Stores Packet, in which the relay with the smaller queue becomes responsible for forwarding it to the destination. The second strategy offers higher aggregate and throughput per user compared to the first, for limited numbers of users.

These results could be used, for example in cellular and sensor networks, to identify the number of required relays to be deployed and allocate the users among relays. Future extensions of this work can include users with non-saturated queues (i.e. users-sources with external random arrivals) and relays with their own packets and priorities for the users. Other interesting extensions consist of relays which are capable of transmitting and receiving at the same time and the investigation of energy consumption in the total network and in particular at the relay nodes.

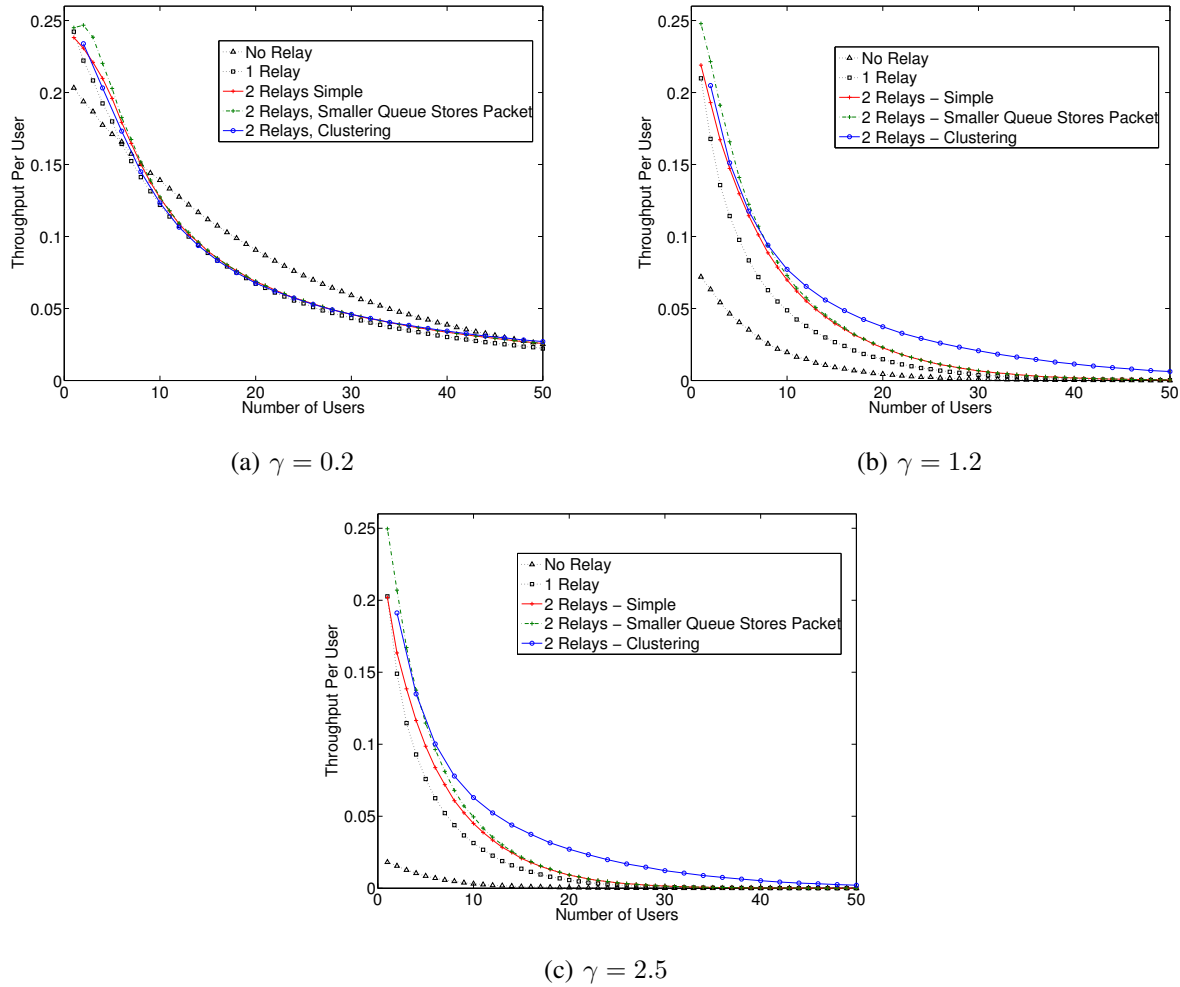


Fig. 10: Throughput per user (in packets per slot) vs. the number of users, for different SINR threshold γ values.

REFERENCES

- [1] G. Papadimitriou, N. Pappas, and A. Traganitis, "Performance issues of multiple-relay cooperation," in *2013 IEEE International Conference on Communications (ICC)*, pp. 6153–6157, June 2013.
- [2] G. Kramer, I. Marić, and R. D. Yates, "Cooperative communications," *Found. Trends Netw.*, vol. 1, pp. 271–425, Aug. 2006.
- [3] J. Laneman, D. Tse, and G. W. Wornell, "Cooperative diversity in wireless networks: Efficient protocols and outage behavior," *IEEE Transactions on Information Theory*, vol. 50, pp. 3062–3080, Dec 2004.
- [4] T. Ng and W. Yu, "Joint optimization of relay strategies and resource allocations in cooperative cellular networks," *IEEE Journal on Selected Areas in Communications*, vol. 25, pp. 328–339, February 2007.
- [5] A. Sadek, K. Liu, and A. Ephremides, "Cognitive multiple access via cooperation: Protocol design and performance analysis," *IEEE Transactions on Information Theory*, vol. 53, no. 10, pp. 3677–3696, 2007.
- [6] B. Rong and A. Ephremides, "Cooperation above the physical layer: The case of a simple network," in *IEEE International Symposium on Information Theory (ISIT)*, pp. 1789–1793, June 2009.
- [7] N. Pappas, A. Ephremides, and A. Traganitis, "Relay-assisted multiple access with multi-packet reception capability and simultaneous transmission and reception," in *IEEE Information Theory Workshop (ITW)*, pp. 578–582, Oct 2011.
- [8] N. Pappas, M. Kountouris, A. Ephremides, and A. Traganitis, "Relay-assisted multiple access with full-duplex multi-packet reception," *IEEE Transactions on Wireless Communications*, vol. PP, no. 99, 2015.
- [9] N. Pappas, J. Jeon, A. Ephremides, and A. Traganitis, "Wireless network-level partial relay cooperation," in *IEEE International Symposium on Information Theory Proceedings (ISIT)*, pp. 1122–1126, July 2012.
- [10] N. Pappas, M. Kountouris, J. Jeon, A. Ephremides, and A. Traganitis, "Network-level cooperation in energy harvesting wireless networks," in *IEEE Global Conference on Signal and Information Processing (GlobalSIP)*, pp. 383–386, Dec 2013.
- [11] K. J. R. Liu, A. K. Sadek, W. Su, and A. Kwasinski, *Cooperative Communications and Networking*. Cambridge University Press, 2009.
- [12] E. C. V. D. Meulen, "Three-terminal communication channels," *Advances in Applied Probability*, vol. 3, no. 1, pp. 120–154, 1971.
- [13] T. Cover and A. Gamal, "Capacity theorems for the relay channel," *IEEE Transactions on Information Theory*, vol. 25, pp. 572 – 584, Sept. 1979.

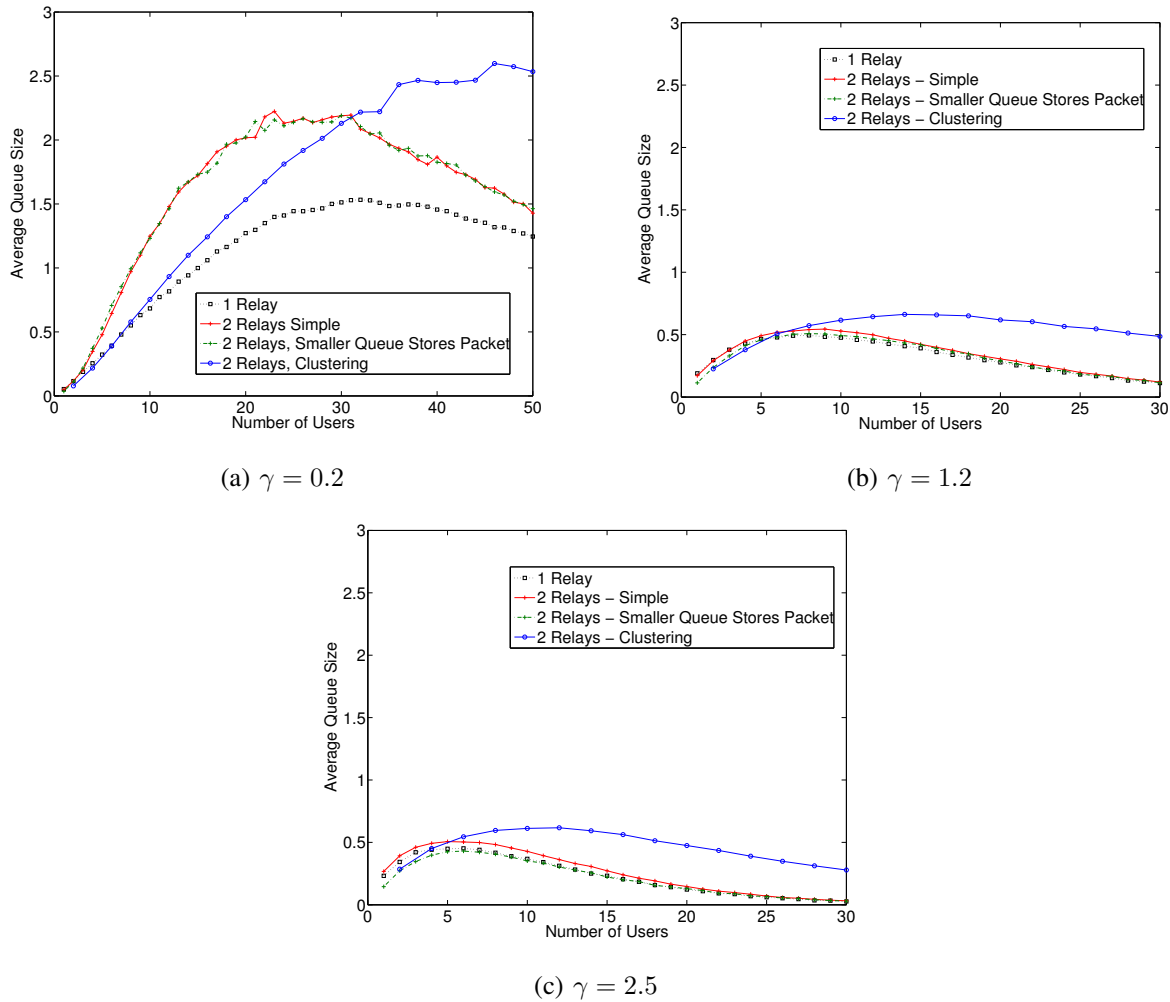


Fig. 11: Average relay queue size (in packets) vs. number of users for different SINR γ values in a system with relays.

- [14] N. Zlatanov, R. Schober, and L. Lampe, "Buffer-aided relaying in a three node network," in *IEEE International Symposium on Information Theory Proceedings (ISIT)*, pp. 781–785, July 2012.
- [15] N. Zlatanov and R. Schober, "Buffer-aided half-duplex relaying can outperform ideal full-duplex relaying," *IEEE Communications Letters*, vol. 17, pp. 479–482, March 2013.
- [16] S. M. Kim and M. Bengtsson, "Virtual full-duplex buffer-aided relaying – relay selection and beamforming," in *24th IEEE International Symposium on Personal Indoor and Mobile Radio Communications (PIMRC)*, pp. 1748–1752, Sept 2013.
- [17] N. Nomikos, T. Charalambous, I. Krikidis, D. Skoutas, D. Vouyioukas, and M. Johansson, "Buffer-aided successive opportunistic relaying with inter-relay interference cancellation," in *24th IEEE International Symposium on Personal Indoor and Mobile Radio Communications (PIMRC)*, pp. 1316–1320, Sept 2013.
- [18] M. Kaneko, P. Popovski, and K. Hayashi, "Throughput-guaranteed resource-allocation algorithms for relay-aided cellular ofdma system," *IEEE Transactions on Vehicular Technology*, vol. 58, pp. 1951–1964, May 2009.
- [19] N. Pappas, A. Traganitis, and A. Ephremides, "Stability and performance issues of a relay assisted multiple access scheme," in *IEEE Global Telecommunications Conference (GLOBECOM 2010)*, pp. 1–5, Dec 2010.
- [20] N. Pappas, M. Kountouris, A. Ephremides, and A. Traganitis, "On the stability region of a relay-assisted multiple access scheme," in *IEEE Information Theory Workshop (ITW)*, pp. 1–8, Sept 2013.
- [21] L. Tong, Q. Zhao, and G. Mergen, "Multipacket reception in random access wireless networks: from signal processing to optimal medium access control," *IEEE Communication Magazine*, vol. 39, pp. 108–112, November 2001.
- [22] S. Ghez, V. S., and S. Schwartz, "Stability properties of slotted aloha with multipacket reception capability," *IEEE Transactions on Automatic Control*, vol. 33, pp. 640–649, Jul 1988.
- [23] V. Naware, G. Mergen, and L. Tong, "Stability and delay of finite-user slotted aloha with multipacket reception," *IEEE Transactions on Information Theory*, vol. 51, pp. 2636–2656, July 2005.
- [24] N. Pappas, A. Ephremides, and A. Traganitis, "Stability and performance issues of a relay assisted multiple access scheme with mpr capabilities," *Computer Communications*, vol. 42, no. 0, pp. 70 – 76, 2014.

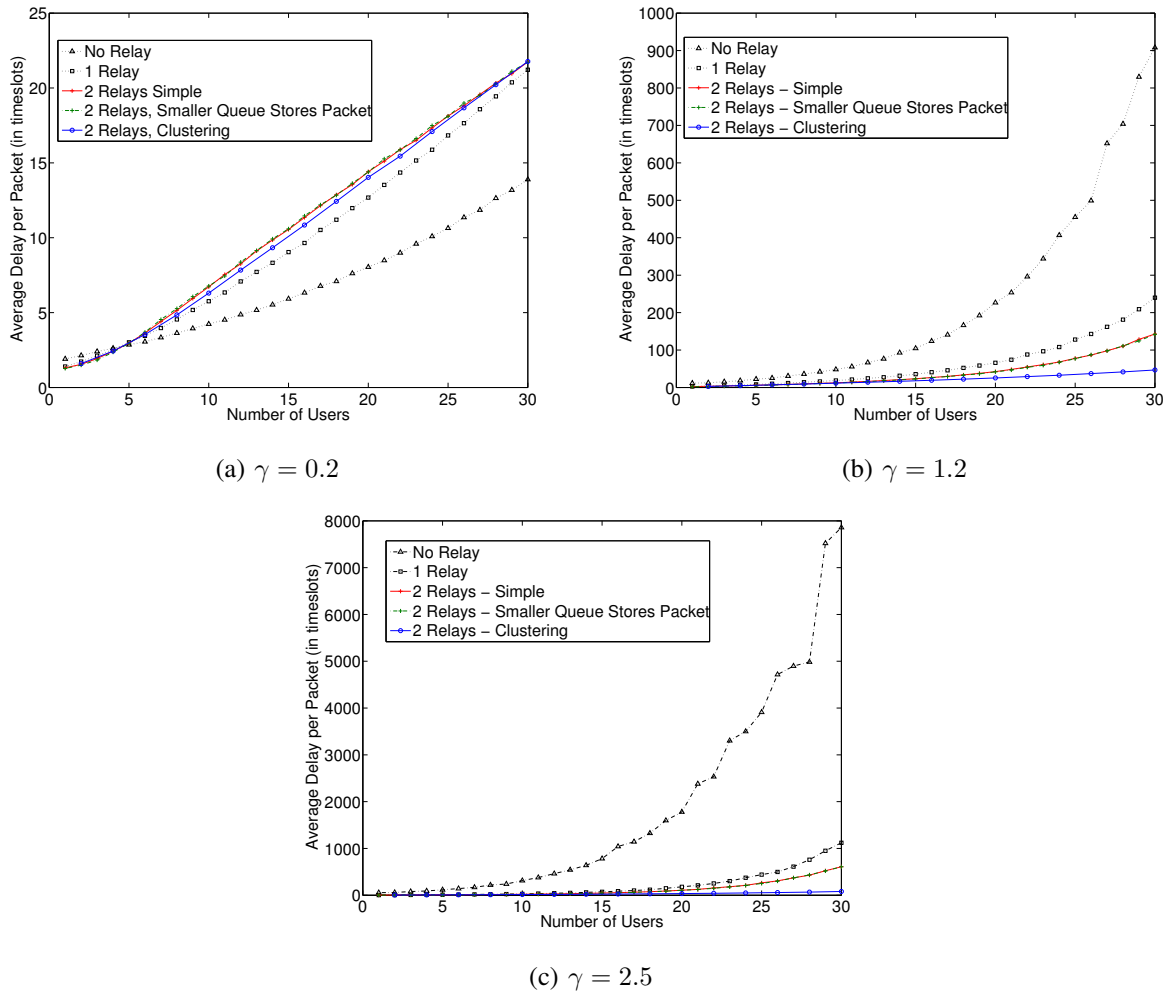


Fig. 12: Average per packet delay (in timeslots) vs. number of users for different SINR γ values in a system with and without relays.

- [25] J. Lu, W. Shu, and M.-Y. Wu, "A survey on multipacket reception for wireless random access networks," *Journal of Computer Networks and Communications*, vol. 2012, Article ID 246359 14 pages, 2012.
- [26] A. Ephremides and B. Hajek, "Information theory and communication networks: an unconsummated union," *IEEE Transactions on Information Theory*, vol. 44, pp. 2416–2434, Oct 1998.
- [27] W. Luo and A. Ephremides, "Stability of n interacting queues in random-access systems," *IEEE Transactions on Information Theory*, vol. 45, pp. 1579–1587, Jul 1999.
- [28] R. Rao and A. Ephremides, "On the stability of interacting queues in a multiple-access system," *IEEE Transactions on Information Theory*, vol. 34, pp. 918–930, Sep 1988.
- [29] Q. He, V. Angelakis, A. Ephremides, and D. Yuan, "Polynomial Complexity Minimum-Time Scheduling in a Class of Wireless Networks," *ArXiv e-prints*, Mar. 2014.
- [30] D. Tse and P. Viswanath, *Fundamentals of Wireless Communication*. New York, NY, USA: Cambridge University Press, 2005.
- [31] W. Szpankowski, "Stability conditions for some distributed systems: Buffered random access systems," *Advances in Applied Probability*, vol. 26, pp. 498–515, Jun. 1994.
- [32] R. M. Loynes, "The stability of a queue with non-independent inter-arrival and service times," *Mathematical Proceedings of the Cambridge Philosophical Society*, vol. 58, pp. 497–520, July 1962.
- [33] G. Dimic, N. Sidiropoulos, and R. Zhang, "Medium access control - physical cross-layer design," *IEEE Signal Processing Magazine*, vol. 21, pp. 40–50, Sept 2004.

Georgios Papadimitriou received his B.S degree in Informatics and Telecommunications Engineering from University of Western Macedonia, Greece in 2010, and M.Sc. degree in Computer Science from University of Crete, Greece in 2012. His M.Sc. thesis was titled Performance Issues of Network Level Cooperation with Multiple - Relays and his supervisor professor was Prof. Apostolos Traganitis, head of the Telecommunications & Networks Laboratory of the Institute of Computer Science (ICS) at the Foundation for Research and Technology-Hellas (FORTH). From September 2014 he works at Ericsson AB, in Stockholm Sweden as Developer at PDU LTE & MS RBS. His main tasks are test analysis, creating test scenarios, evaluating test results and troubleshooting of faults, as well as legacy system verification testing.

Nikolaos Pappas received his BSc degree in Computer Science from University of Crete, Greece in 2005, and MSc degree in Computer Science from University of Crete, Greece, in 2007. He also obtained his BSc degree in Mathematics from University of Crete, Greece in 2012. He holds a PhD degree from the Department of Computer Science of the University of Crete, Greece in 2012. From 2005 to 2012, he was a graduate research assistant with the Telecommunications and Networks Laboratory of the Institute of Computer Science of the Foundation for Research and Technology, Hellas (FORTH) and he has been a visiting scholar of the Institute of Systems Research at the University of Maryland in College Park. From September 2012 to March 2014, he was a postdoctoral researcher at the Department of Telecommunications, at Supélec, France. Since March 2014 he is at the University of Linköping at Norrköping Campus as a Marie Curie Fellow (IAPP). His main research interests are in the field of wireless communication networks with emphasis on the stability analysis, energy harvesting networks, network-level cooperation, network coding and stochastic geometry. He is an Editor for the IEEE Communications Letters.

Apostolos Traganitis holds a M.S. (1972) and a PhD (1974) degree from Princeton University and the Diploma in Electrical Engineering (1970) from the National Technical University of Athens. He is a professor in the Dept. of Computer Science of the University of Crete, having served as its Chairman from 2000 to 2002. He is also the Head of the Telecommunications and Networks Laboratory of the Institute of Computer Science of the Foundation for Research and Technology, Hellas (FORTH). During 1993 and 1994 he was a Visiting Research Fellow at the Center of Satellite and Hybrid Communications Networks (CSHCN) of the Institute of Systems Research (ISR), University of Maryland. Previously he has been a Senior Researcher in the Hellenic Navy Research Laboratory (GETEN), in charge of the Electronic Warfare Unit. His interests are in the areas of Digital Communications, Wireless Networks, Communications Security, Hardware Design and Biomedical Engineering.

Vangelis Angelakis holds an MSc('04) and a PhD('08) in Computer Science from the University of Crete, Greece. Presently, he is an Assistant Professor in Mobile Telecommunications at the Department of Science and Technology, Linköping University. His current research is centered on Wireless Networks' resource allocation. Dr Angelakis has been a research assistant at the Institute of Computer Science (ICS) of the Foundation for Research And Technology – Hellas (FORTH), Greece since 2001. In 2005 he was a visiting research associate at the Institute for Systems Research of the University of Maryland in College Park, USA. From 2008 he was a postdoctoral researcher with the Telecommunications and Networks laboratory of FORTH-ICS, until 2009 when he joined Linköping University. Since then he has been a visiting researcher in the UK (RANPLAN Ltd), and China (Huazhong University of Science and Technology). He is an associate editor of the Journal of Communications and has received support from national funding bodies in Greece, Sweden, and the EU within FP7.